

AODisaggregation: toward global aerosol vertical profiles



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Motivation

Design of a prior over b_{ext}

Connecting $\varphi(x|h)$ to observations

Experiments

Conclusion

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- ▶ Uncertainty in magnitude of forcing due to ACIs comes from:
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 2. Uncertainty in estimation of present day forcing

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Objective

Try to reconstruct aerosol vertical profiles using AOD

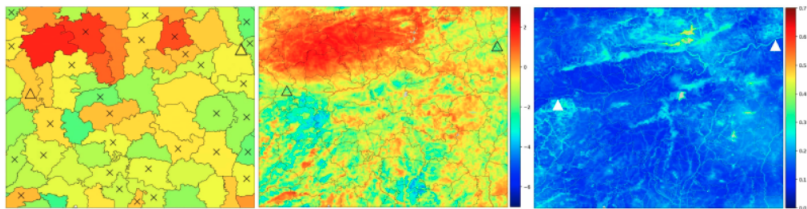


Figure 2: Triangle denotes approximate start and end of river location, crosses denotes non-train set bags. Malaria incidence rate λ_i^a is per 1000 people. **Left, Middle:** $\log(\hat{\lambda}_i^a)$, with constant model (Left), and VBAgg-Obj-Sq (tuned on \mathcal{L}_1^s) (Middle). **Right:** Standard deviation of the posterior v in (9) with VBAgg-Obj-Sq.

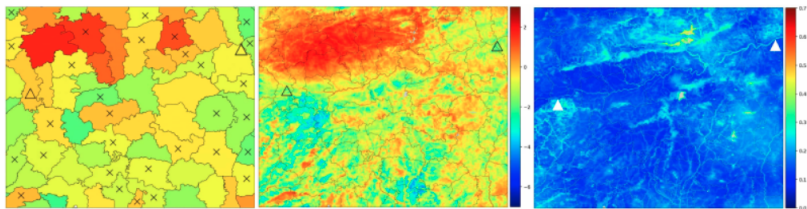


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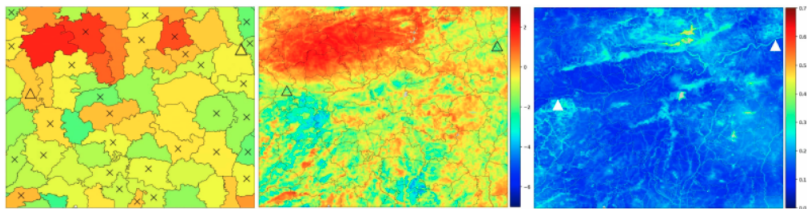


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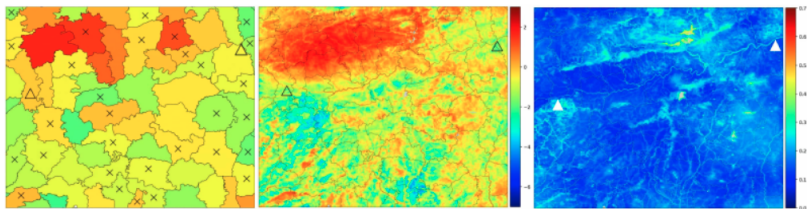
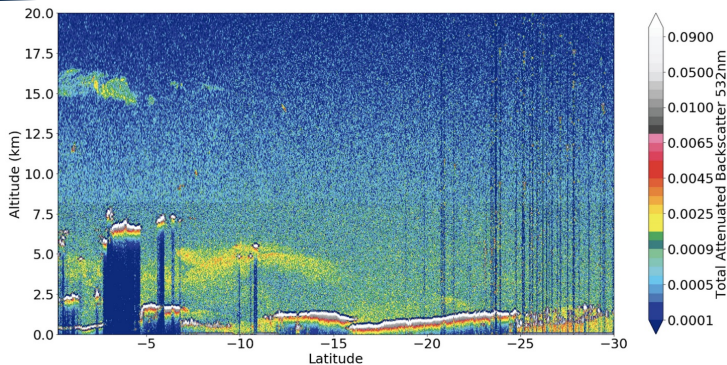


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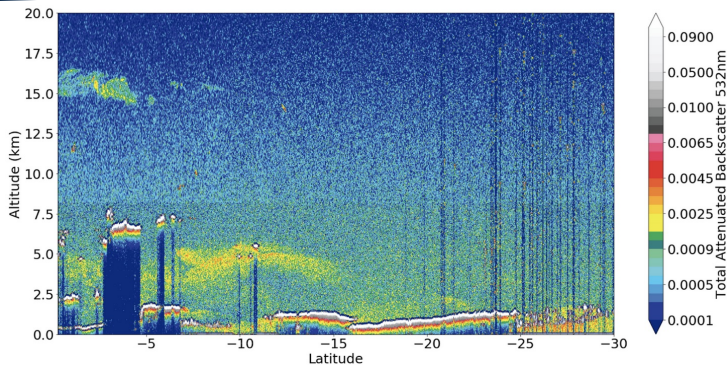
- ▶ **Observations:** $\text{rate}_{\text{region}}$ and $x_{\text{fine-grid}}$
- ▶ **Goal:** Infer $\text{rate}_{\text{fine-grid}}$ as a function of $x_{\text{fine-grid}}$

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- ▶ **Observations:** τ_{column} and x_{3D}
- ▶ **Goal:** Infer b_{ext} as a function of x_{3D}

- ▶ Use simple, readily available predictors such as pressure, temperature, humidity \rightarrow reanalysis data.

For example, for a given altitude h we can take

$$x = (t, \text{lat}, \text{lon}, P, T, \text{RH}) \quad (1)$$

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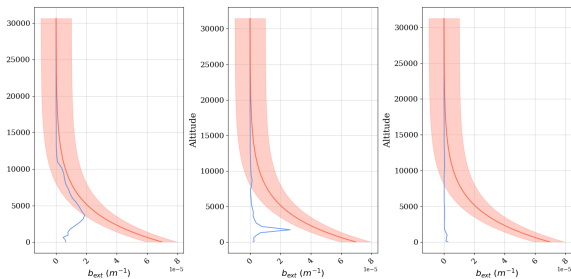
Objective

Using observations of AOD and vertically-resolved meteorological predictors, we want to estimate aerosol extinction profiles.

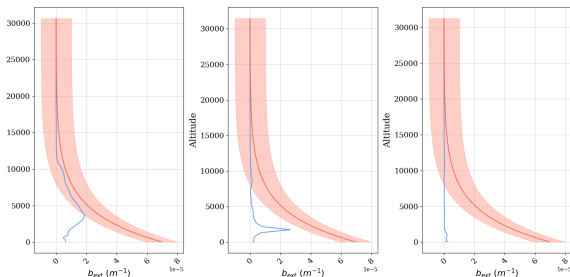
Design of a prior over b_{ext}



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- ▶ Rough approximation but captures a key structure: most aerosol lie in *boundary layer* ($< 2 \text{ km}$)

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Expect relationship between $x|h$ and $b_{\text{ext}}(h)$ to be non-trivial and highly non-linear \Rightarrow learn the weighting $w(x|h)$

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- ▶ Reflect this with Bayesian design of $w(x|h)$

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$$\psi > 0 \tag{5}$$

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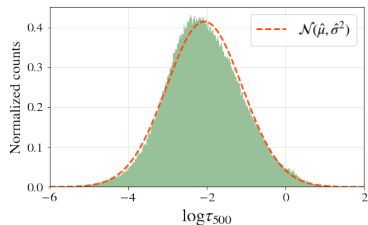
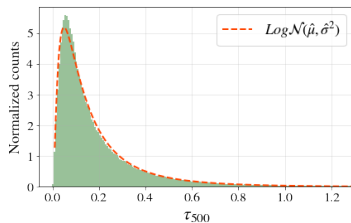
- ▶ Simple choice $\psi = \exp$
 - ▶ $\psi \circ f$ describes expressive range of probability distribution over complex positive functions
 - ▶ Remains interpretable (kernel user-specified determines covariance and functional smoothness)
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Connecting $\varphi(x|h)$ to observations

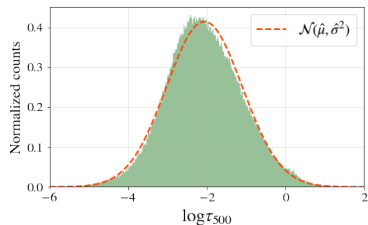
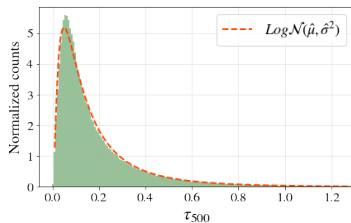


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$$\tau | \mu, \sigma \sim \mathcal{LN}(\mu, \sigma) \quad (6)$$

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Observation model

$$\tau|\eta \sim \mathcal{LN}\left(\log \eta - \frac{\sigma^2}{2}, \sigma\right) \quad (7)$$

$$\eta = \int_0^H \varphi(x|h) dh \quad (8)$$

With multiple observations τ_1, \dots, τ_n , scale parameter $\sigma > 0$ assumed shared among columns but η (or μ) is column-specific.

Model formulation for the i^{th} atmospheric column

Observation Model:

$$\tau_i | \eta_i \sim \mathcal{LN} \left(\log \eta_i - \frac{\sigma^2}{2}, \sigma \right)$$

$$\eta_i = \int_0^H \varphi(x_i|h) dh$$

Prior:

$$\varphi(x_i|h) = \psi(f(x_i|h))e^{-h/L}$$

$$f \sim \text{GP}(m, k)$$

τ_i	Observed AOD
\mathcal{LN}	Log-normal distribution
η_i, σ	Mean and scale parameters
φ	Prior for b_{ext}
$x_i h$	Input covariates at altitude h
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- **Objective:** Infer distribution of $\varphi(x|h) | \underbrace{\tau_1, \dots, \tau_n}_{\tau}$

- ▶ Actually... $f(x|h)|\boldsymbol{\tau}$
- ▶ Access to posterior distribution $p(f|\boldsymbol{\tau})$ allows to compute predictive mean and variance of φ at input $x|h$ following

$$\mathbb{E}[\varphi(x|h)|\boldsymbol{\tau}] = \int \psi(f)e^{-h/L}p(f|\boldsymbol{\tau}) df$$
$$\text{Var}(\varphi(x|h)|\boldsymbol{\tau}) = \mathbb{E}[\varphi(x|h)^2|\boldsymbol{\tau}] - \mathbb{E}[\varphi(x|h)|\boldsymbol{\tau}]^2$$

- ▶ Can be estimated with Monte-Carlo (and admits closed form for $\psi = \exp$)

Problem

$$p(f|\boldsymbol{\tau}) = \frac{p(\boldsymbol{\tau}|f)p(f)}{\underbrace{\int p(\boldsymbol{\tau}|f)p(f) df}_{\text{intractable}}}$$

Solution

- ▶ Approximate $p(f|\boldsymbol{\tau})$ (variational approximation)
- ▶ Approximation scheme allows for sparse representation which scales to very large number of data points

Experiments



	Name	Notation	Dimensions
<i>Predictors</i>	Temperature	T	$(t, \text{lat}, \text{lon}, \text{lev})$
	Pressure	P	$(t, \text{lat}, \text{lon}, \text{lev})$
	Relative humidity	RH	$(t, \text{lat}, \text{lon}, \text{lev})$
	Vertical velocity	ω	$(t, \text{lat}, \text{lon}, \text{lev})$
<i>Response</i>	AOD 550nm	τ	$(t, \text{lat}, \text{lon})$
<i>Groundtruth</i>	Extinction coefficient 533nm	b_{ext}	$(t, \text{lat}, \text{lon}, \text{lev})$

Table 1: Gridded variables from ECHAM-HAM simulation data. The grid includes 8 time steps (t), 96 latitude levels (lat), 192 longitude levels (lon) and 31 vertical pressure levels (lev). Our objective is to vertically disaggregate the response τ using the vertically resolved predictors (T, P, RH, ω) and spatiotemporal columns locations ($t, \text{lat}, \text{lon}$).

- Total of $8 \times 96 \times 192 = 147\,456$ columns.

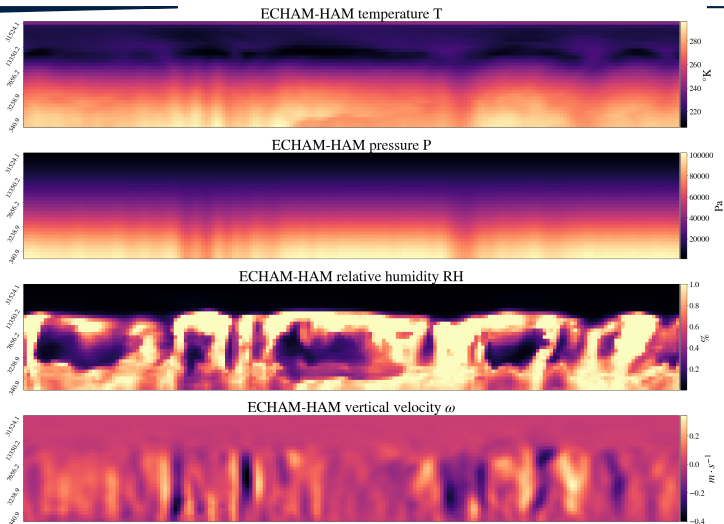


Figure 1: Vertical slices at latitude 51.29° of meteorological predictors

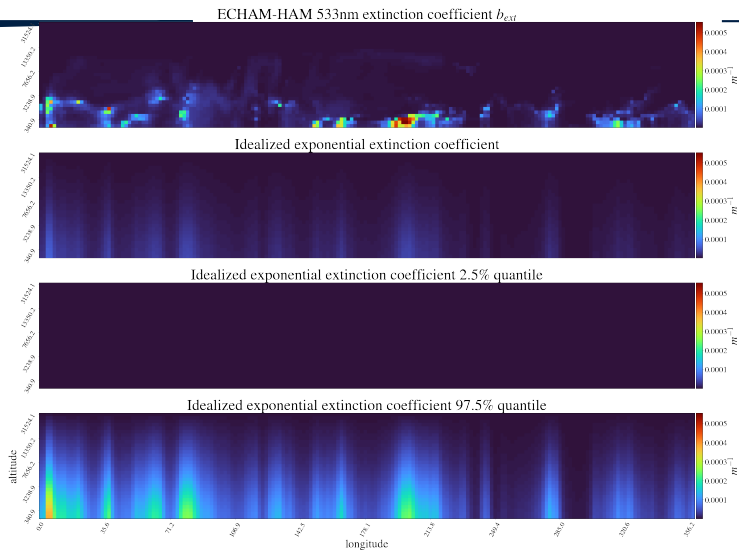


Figure 2: Vertical slices at latitude 51.29° of idealized profiles

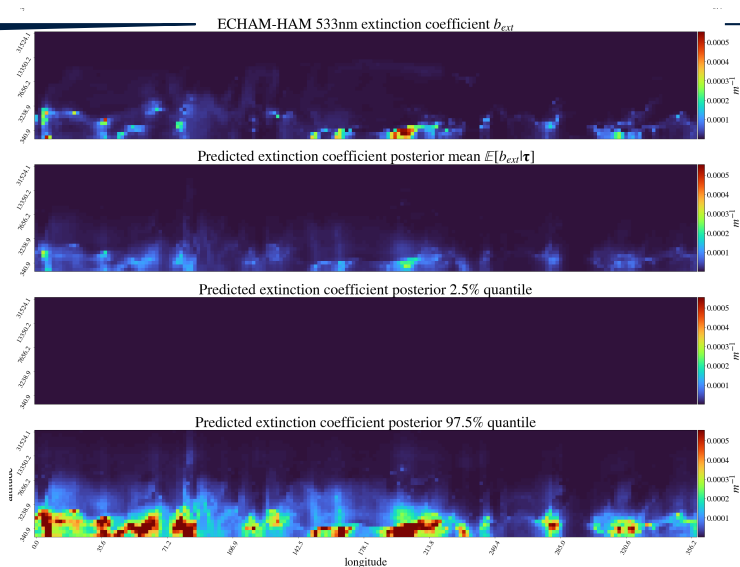


Figure 3: Vertical slices at latitude 51.20° of predicted profiles

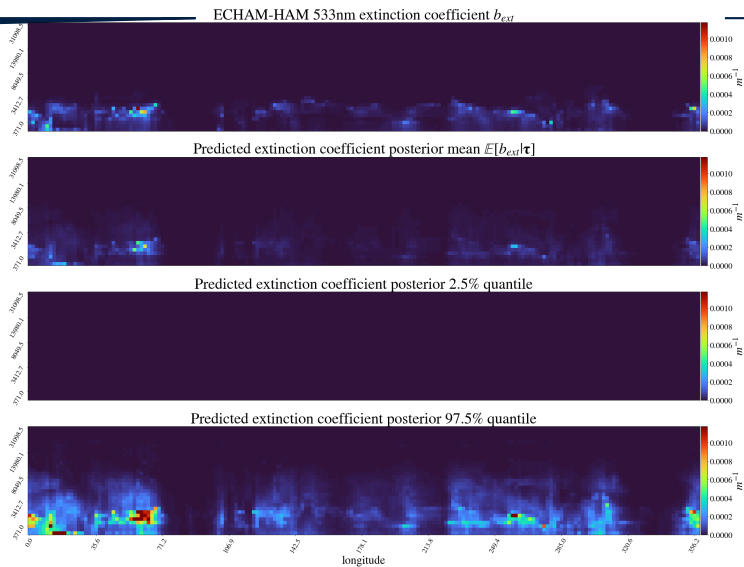


Figure 4. Vertical slices at latitude -0.93° of predicted profiles

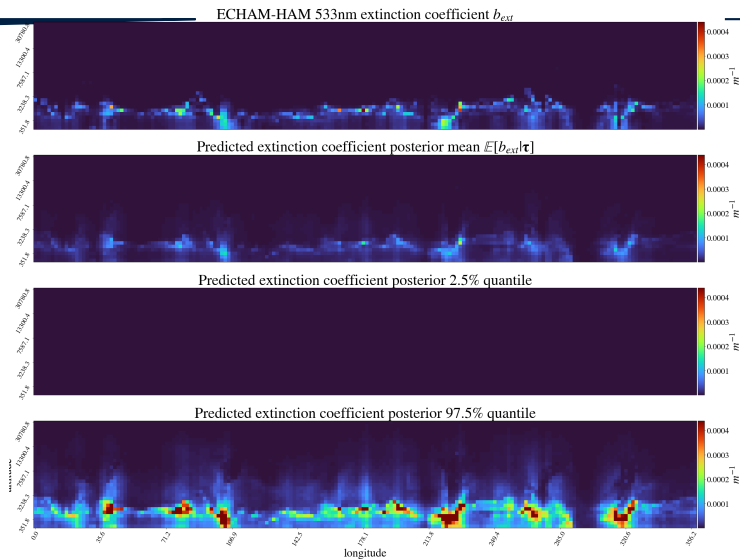


Figure 5: Vertical slices at latitude -38.2° of predicted profiles

Table 2: Scores of our method (Our) compared to an idealized exponential baseline (Ideal)

<i>Region</i>	Method	RMSE (10^{-5})	Corr (%)	Bias (10^{-6})	Bias98 (10^{-5})
<i>Entire column</i>	Our	3.29 ± 0.02	70.9 ± 0.4	-0.167 ± 0.105	-0.646 ± 0.151
	Ideal	4.10	51.2	-2.40	-4.08
<i>Boundary layer</i>	Our	6.06 ± 0.03	69.8 ± 0.5	-1.25 ± 0.45	-4.64 ± 0.32
	Ideal	7.55	53.6	-12.9	-11.7

<i>Region</i>	Method	ELBO	Calib95 (%)	ICI (10^{-2})
<i>Entire column</i>	Our	13.1 ± 0.1	94.9 ± 0.1	5.29 ± 0.59
	Ideal	13.1	96.0	5.05
<i>Boundary layer</i>	Our	10.6 ± 0.1	98.8 ± 0.1	8.27 ± 0.29
	Ideal	10.2	93.5	19.1

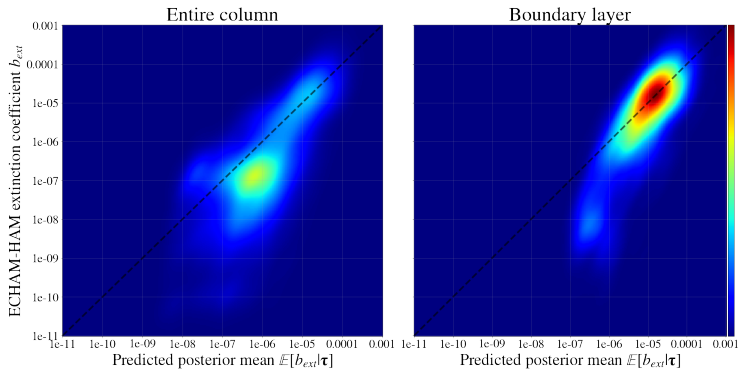


Figure 6: Density plots of groundtruth extinction coefficient values against predicted posterior mean extinction coefficient; **Left:** entire column; **Right:** boundary layer only

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 - ▶ Methodological extensions (use multiple wavelengths, allow unmatched data setting)
 - ▶ Different use case: investigation on aerosol mode/species contribution to extinction using model data only
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Preprint

*Shahine Bouabid, Duncan Watson-Parris, Sofija Stefanović,
Athanasios Nenes, Dino Sejdinovic.
AODisaggregation: toward global aerosol vertical profiles
arXiv preprint arXiv:2205.04296.*

Code and Data

<https://github.com/shahineb/aodisaggregation>
